**Title:** Marxan vs ILP

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**Abstract**

**Introduction**

Systematic conservation planning (SCP) is a rigorous, repeatable, and structured approach to designing new protected areas that efficiently meet conservation objectives (Margules and Pressey 2000). Historically, conservation decision-making has often evaluated parcels opportunistically as they became available for purchase, donation, or under threat. Although purchasing such areas may improve the status quo, such decisions may not substantially enhance the long-term persistence of target species or communities. Faced with this realization, conservation planners began using decision support tools to help simulate alternative reserve designs over a range of different biodiversity and management goals and, ultimately, guide protected area acquisitions and management actions. Due to the systematic, evidence-based nature of these tools, conservation prioritization can help contribute to a transparent, inclusive, and more defensible decision-making process.

There are two main approaches to solving optimization problems of this type. First, integer linear programming (ILP), which minimizes or maximizes an objective function (a mathematical equation describing the relationship between actions and out-comes) subject to a set of constraints and conditional on the decision variables (the variables corresponding to the selection of actions to implement) being integers. Second, solutions can be found using heuristic methods such as simulated annealing (SA; Kirkpatrick et al., 1983), which iteratively, stochastically explore the state-space of the decision variables. There are numerous other heuristics (e.g. ranking procedures, genetic algorithms, and mixtures of these approaches) that could also be used. Here, we focus on SA because it is the most widely used heuristic in the conservation planning literature in the form of the conservation planning software Marxan (Ball et al., 2009; Watts et al., 2009) and, unlike deterministic heuristics such as ranking, it is possible that SA could find an optimal solution to any problem.

Marxan is the most widely used SCP software globally, being used in 184 countries to build marine and terrestrial conservation systems and is the global leader in conservation land and sea use planning software. Marxan uses the heuristic approach of similated annealing to find ‘near optimal’ solutions to SCSP problems. Recent developments in computational capacity and algorithms has made it possible to solve the SCP problems Marxan solves with integer linear programming (Beyer et al. 2016). Building on Beyer et al. (Beyer et al. 2016), we created a software package for the R statistical software called prioritizr, that can solve Marxan type problems using integer linear programming (Hanson et al. 2019).

Here, we are using a case study from Western North America to compare Marxan (simulated annealing) and prioritizr (integer linear programming) to ask the following questions:

1. What is required to parameterize i) Marxan, ii) prioritizr using an open source solver, and iii) prioritzr using a proprietary solver?
2. How do processing time differ between the three approaches tested?
3. How cost effective, in $ values, are the three approaches tested?

**Methods**

*Study area*

We focused on a 27,250 km2 portion of the Georgia Basin, Puget Trough and Willamette Valley of the Pacific Northwest region spanning the US and Canada (Fig. 1), corresponding to the climate envelope indicative of the Coastal Douglas-fir (CDF) Biogeoclimatic zone in southwestern British Columbia (Meidinger and Pojar 1991). Land cover in the region is diverse, with approximately 57% of the land in forest, 8% as savanna or grassland, 5% in cropland, and 10% being urban or built.

*Data Layers*

*Biodiversity data.* Our prioritizations were run with eBird data, which is a citizen-science effort that has produced the largest and most rapidly growing biodiversity database in the world (Hochachka et al. 2012, Sullivan et al. 2014). From the 2013 eBird Reference Dataset (<http://ebird.org/ebird/data/download>) we used a total of 12081 checklists in our study area, then filtered these checklists to retain only those <1.5 hours in duration, <5 km travelled, and a maximum of 10 visits to a given location (unpublished R code; Hochachka, pers. com.). Sampling locations <100 m apart were collapsed to one location, yielding 5470 checklists from 2160 locations, visited from 1-10 times and 2.53 times on average. Following (Schuster et al. 2014, 2017) we used a combination of quantitative models and expert elicitation to identify which species were associated either with forest habitat or with human-dominated habitat, such as built or residential land (Supplemental Material methods, Supplementary Table 1). For further details see Rodewald et al. (XXXX).

*Cadastral layer and land cost*. We incorporated spatial heterogeneity in land cost (Ando et al. 1998, Polasky et al. 2001, Ferraro 2003, Naidoo et al. 2006) in our plan by using cadastral data and 2012 land value assessments from the Integrated Cadastral Information Society of BC, resulting in 193,623 polygons for BC (Schuster et al. 2014). Cadastral data, including tax assessment land values from Washington State came from the University of Washington’s Washington State Parcel Database (<https://depts.washington.edu/wagis/projects/parcels/>; Version: StatewideParcels\_v2012n\_e9.2\_r1.3; Date accessed: 2015/04/30), as well as San Juan County Parcel Data with separate signed user agreement. The combined cadastral layer included 1.92M polygons. Cadastral data, including tax assessment land values from Oregon State had to be sourced from individual counties, which included Benton, Clackamas, Columbia, Douglas, Lane, Linn, Marion, Multnomah, Polk, Washington and Yamhill. The combined cadastral layer for Oregon included 605,425 polygons.

*Spatial prioritization approach*

Here we use the concept of systematic conservation planning (Margules and Pressey 2000), to inform choices about areas to protect, in order to optimize outcomes for biodiversity while minimizing societal costs (McIntosh et al. 2017). To achieve the goal to optimize the trade-off between conservation benefit and socioeconomic cost, i.e. to get the most benefit for limited conservation funds, we strive to minimize an objective function over a set of decision variables, subject to a series of constraints.

Marxan formulation

Integer linear programming (ILP) is the subset of optimization algorithms used here to solve reserve design problems. The general form of an ILP problem can be expressed in matrix notation as:

Where x is a vector of decision variables (in our case, whether to prioritize an individual planning unit), c and b are vectors of known coefficients, and A is the constraint matrix. In the minimum set cover problem, c is a vector of costs for each planning unit, b a vector of targets for each conservation feature, the relational operator would be ≥ for all features, and A is the representation matrix with Aij=rij, the representation level of feature i in planning unit j. We set an objective to find the solution that fulfills all the targets and constraints for the smallest area, which we use as our measure of cost (Beyer et al. 2016).

*Scenarios investigated*

**Results**

**Discussion**

**Conclusion**

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